

# Exploring Number Theory Applications in Cryptography and Security Analysis

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**Abstract:** Number theory a subject of pure mathematics is essential to security applications and cryptography. This study examines number theory's underlying ideas and practical applications to ensure data privacy, soundness, and correctness in current cryptographic systems. Primordial numbers, modular arithmetic, and integer characteristics are introduced in the essay. This research clearly explores how prime numbers aid key exchange methods and cryptographic key creation. Modular exponentiation, which underpins many encryption and decryption algorithms, is also addressed in modular arithmetic. The paper also considers using number theory to create digital signatures that verify data. It studies the mathematical foundations of digital signature algorithms like the Elliptic Curve Digital Signature Algorithm (ECDSA) and the RSA signature scheme, which use modular arithmetic and prime numbers to verify digital document authenticity and integrity. The limits and uses of number theory-based encryption are also examined. Advances in computer hardware and computational complexity affect system security. The paper examines post-quantum cryptography, which seeks to create cryptographic algorithms that are secure even with quantum computers.

**Keywords:** Modular arithmetic, Prime numbers, Factorization.

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